

METHOD OF OPERATING A HYBRID POWER SYSTEM  
WITHIN A STATE OF CHARGE WINDOW

5 FIELD OF THE INVENTION

This invention generally relates to hybrid power systems employing fuel cells, and deals more particularly with a method of controlling system operation within a state-of-charge window of a battery  
10 pack in a manner that reduces use of the fuel cell.

BACKGROUND OF THE INVENTION

Hybrid power systems employing multiple power energy sources require careful control of system  
15 components in order to coordinate the delivery of power from the sources to system loads. These loads can vary widely in magnitude, and occur unexpectedly in time, particularly in hybrid powered vehicles. Hybrid systems using fuel cells and battery packs as energy sources to  
20 power vehicles must be closely controlled to assure adequate reserve power is available under a variety of conditions, while also conserving fuel to maximize mileage.

25 In order to assure that adequate reserve power is present in the battery pack and that proper charging and discharging of the battery is maintained, the state-of-charge (SOC) of the battery is monitored, and charging and discharging are controlled so that the SOC  
30 remains within an acceptable range or "window". When the SOC is low, the fuel cell may be called upon to produce power in order to charge the battery to keep the

SOC within the desired window. The efficiency of the fuel cell in producing the power needed to recharge the battery is dependant in part on the voltage region in which it is operating. Accordingly, the fuel cell  
5 may be called to recharge the battery under conditions in which the fuel cell is operating at less than maximum efficiency.

Accordingly, a need exists for a method of  
10 controlling the operation of a hybrid power system which maintains the SOC of the battery within a desired window, while minimizing the use of the fuel cell for battery charging.

#### 15 SUMMARY OF THE INVENTION

According to one aspect of the invention, a method is provided for controlling the operation of hybrid power system having a fuel cell and a charge carrier such as a battery pack. The method includes the  
20 steps of determining the state of charge of the charge carrier; setting the power output of the charge carrier to a first value if the power required by the load is less than the maximum power available to be supplied from the fuel cell; and, setting the power output of the  
25 charge carrier to a second value if the power required by the load is equal to or greater than the maximum power available to be supplied from the fuel cell.

According to another aspect of the invention,  
30 a method is provided for use in controlling the operation of a hybrid power system having a battery pack and a fuel cell, which maintains the battery pack's state-of-charge within a preselected range. The method includes the steps of monitoring the battery pack's

state of charge; determining the amount of power required by the load; determining the amount of power being supplied by the fuel cell; and, setting the power output of the battery pack based on the determined  
5 amounts of power.

An important feature of the invention is that minimum use is made of the fuel cell to maintain the battery pack's SOC charge within a desired window. The  
10 control strategy shares the power sourced from the fuel cell and the battery pack to the load in a manner that optimizes the use of the fuel cell, thereby conserving fuel and lengthening the service life of the battery.

15 Another feature of the invention is that the power output of the battery pack is regulated based on load demand relative to the fuel cell's ability to satisfy this demand. By reducing the amount of power supplied to the load from the battery pack at certain  
20 times and using the fuel cell to satisfy any remaining portion of the demanded power, fuel cell use is optimized while maintaining the charge of the battery pack within a desired range.

25 These and other features and advantages of the present invention may be better understood by considering the following details of a description of a preferred embodiment of the invention. In the course of this description, reference will frequently be made to  
30 the attached drawings.

#### BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 is a block diagram of a hybrid fuel power system operated in accordance with the method of the invention;

Fig. 2 is a waveform diagram showing the lumped system load current in the system of Fig. 1 when operated in accordance with the method of the invention;

Figs. 3a and 3b are waveform diagrams, respectively showing the voltage and current output of the fuel cell forming part of the system depicted in Fig. 1, based on calculated battery pack power;

Fig. 4 is a waveform diagram showing the power output of the fuel cell;

Fig. 5 is a waveform diagram showing the power output by a battery pack forming part of the charge carrier depicted in Fig. 1;

Fig. 6 is a waveform diagram showing the state of charge for the battery pack; and,

Fig. 7 is a flow chart showing the steps of the method of the present invention.

#### DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

Referring first to Fig.1, a fuel cell-based hybrid power system includes a fuel cell 10 and a d.c. power source 12 coupled in parallel with each other to supply power to system loads 14. The fuel cell 10 may be any of various types, such as a PEM (polymer

electrolyte membrane), or a SOFC (solid oxide fuel cell) using any of a variety of fuels. These fuel cells are characterized by a voltage-current polarization curve (not shown), which dictates the operating regime of the fuel cell. This polarization curve shows an increasing power output as the fuel cell voltage is decreased to a maximum power boundary point after which the power output decreases with decreasing voltage. Another characteristic of these fuel cells is the approximately linear decrease in fuel conversion efficiency as the voltage is decreased. Thus, in order to operate the fuel cell efficiently, it would be desirable to maintain a lower threshold on the voltage: the maximum power boundary point. For purposes of this description, it is assumed the fuel cell 10 can be operated at any point along its polarization curve.

The d.c. energy source 12 includes a high voltage charge carrier 16 coupled in series with a power converter 18. The charge carrier 16 may include either a battery pack having a plurality of battery cells connected with each other, an ultracapacitor for storing electrical energy, a flywheel or other device for storing electrical power, or a combination of these devices. For illustration and sake of simplicity in explaining the invention herein, however, the charge carrier 16 will sometimes be referred to as a battery pack or battery. The power converter 18 is a conventional, bidirectional device that converts the power supplied by the charge carrier 16 into a form that is compatible with the requirements of the system loads 14. Specifically, the power converter converts the voltage and current supplied by the charge carrier 16

into levels that match the voltage on a parallel bus that supplies power to the system loads 14.

5       The system loads 14 may include a wide variety  
of devices that utilize electric power, which are  
coupled in parallel with the d.c. power source 12 and  
the fuel cell 10. For example, in the case of a vehicle  
application of the hybrid fuel power system, the system  
loads 14 may include wheel drive motors, motors driving  
10 vehicle accessories, regenerative braking devices, and  
other power using or power generating loads which have a  
negative (source or sink) or positive signed power.  
Similarly, the charge carrier 16 can have a negative  
(discharging) or positive (charging) sign.

15

      The relative amount of power stored in the  
battery pack (charge carrier 16) is often referred to as  
its "state-of-charge" (SOC), i.e. the amount of stored  
energy expressed as a percentage of the battery pack's  
20 total ampere-hour capacity. In order to efficiently  
charge and discharge, the battery must be maintained  
within a charge range known as an SOC window that is  
adequate to meet the power requirements of the power  
system in which the battery is utilized. The power  
25 requirements of the system loads 14 are sourced either  
from the battery 16 or the fuel cell 10, depending on a  
variety of conditions, including the size of the load  
demand and the SOC of the battery. Typically, when the  
battery SOC drops to a threshold value at the lower end  
30 of the SOC window, the fuel cell 10 is activated to  
charge the battery until the battery SOC reaches a  
higher limit, near the upper end of the SOC window.

In accordance with the present invention, a method is provided for controlling the power sharing between the fuel cell 10 and the battery 16 sourced to the system loads 14 which optimizes the use of the fuel cell 10, and therefore reduces fuel consumption. The control strategy employed by the inventive method, in part, monitors the SOC of the charge carrier 16 and controls the power output by the charge carrier 16 based on the monitored SOC, and the system load demand.

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In further explaining the control method of the present invention and its derivation, the following symbols and nomenclature will be used:

- 15  $P_{FC}(k)$  = Fuel Cell Power
- $P_{FC}^{MAX}$  = Fuel Cell Maximum Power Output
- $V_{FC}(k)$  = Fuel Cell Voltage
- $I_{FC}(k)$  = Fuel Cell Current
- $V_{FC}^{MAX}$  = Fuel Cell Maximum Voltage
- 20  $V_{FC}^{MIN}$  = Fuel Cell Minimum Voltage
- $V_{FC}^{MAX\ POWER}$  = Fuel Cell Voltage Maximum Power Point
- $P_{LOADS}(k)$  = Lumped System Loads Power
- $V_{LOADS}(k)$  = Lumped System Loads Voltage
- $I_{LOADS}(k)$  = Lumped System Loads Current
- 25  $P_{CC}(k)$  = Charge Carrier Power
- $C(k)$  = Charge Carrier SOC
- $C_{NOM}$  = Charge Carrier Nominal SOC
- $C_{MIN}$  = Charge Carrier SOC Minimum
- $C_{MAX}$  = Charge Carrier SOC Maximum
- 30  $S$  = SOC scaling constant
- $\eta_{PC}$  = Power Converter Efficiency
- $\eta_{CC}(k)$  = Charge Carrier Lumped Efficiency
- $e_{CC}$  = Charge Carrier Lumped Charge/Discharge Efficiency
- $\eta_{FC}(k)$  = Fuel Cell Efficiency

- A = Fuel Cell polarization curve model constant  
 B = Fuel Cell polarization curve model constant  
 $V_0$  = Voltage at which ohmic Region Linear Curve  
 Intercepts with Zero Current  
 5  $S_0$  = Slope of the Ohmic Region Linear Curve

The control method is carried out by setting the charge carrier 16 power output, based on the previous SOC level, to the following

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$$P_{CC}(k) = (n_{CC}(k) * V_{FC}^{MAX}) / (2 * S * V_{FC}(k)) + C(k-1) - C_{NOM}$$

if the power required by the system loads 14 is less than the maximum power available from the fuel cell 10 and

15

$$P_{CC}(k) = -(P_{LOAD}(k) + P_{FC}^{MAX})$$

if the power required by the system loads 14 is equal to or greater than the maximum power available from the fuel cell 10 and the fuel cell is operating at its maximum power output. Simulation testing has shown that this control method considerably decreases the power supplied by the fuel cell 10 over time, when compared to the use of the charge carrier 16 only as an additional power source for fuel cell short falls, and as a sink for regenerative braking. This control strategy would therefore lead to a proportional increase in fuel economy.

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A fuel cell polarization curve can be modeled as an exponential over the operating range of the fuel cell using two model constants A and B.

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$$I_{FC}(k) = A * \exp(-(V_{FC}^2)/B) \quad (1)$$

The constants can be found by fitting equation (1) with actual fuel cell polarization data using a variety of



curve fitting methods. Fuel cell efficiency can also be modeled as a linear function of the fuel cell voltage.

$$n_{FC}(k) = V_{FC}(k) / V_{FC}^{MAX} \quad (2)$$

It is assumed that Charge Carrier and Power Converter efficiencies are constant. The battery pack efficiency is set based on the signum of the charge carrier power.

$$n_{CC}(k) = \begin{cases} (n_{PC} * e_{CC}) ; \text{sgn}(P_{CC}(k)) \geq 0 \\ 1/(n_{PC} * e_{CC}) ; \text{otherwise} \end{cases}$$

The power sharing relation between the different components of the system can be expressed as follows:

$$- P_{LOADS}(k) = P_{FC}(k) * n_{FC}(k) + P_{CC}(k) * n_{CC}(k) \quad (3)$$

The control strategy sought is one that minimizes the power output from the fuel cell, which in turn minimizes the fuel used, while maintaining operation within a pre-defined charge carrier SOC window.

$$C(k) \in [C_{MIN}, C_{MAX}]$$

$$C(k) = C(k-1) - P_{CC}(k) \quad (4)$$

Equation (3) can be rewritten as a function of the fuel cell power.

$$P_{FC}(k) = -(1/n_{FC}(k)) * (P_{LOADS}(k) + P_{CC}(k) * n_{CC}(k)) \quad (5)$$

Given the constraints previously mentioned, it is desirable to optimize the choice of  $P_{CC}(k)$ . Thus, a minimization problem is set up incorporating the SOC constraint explicitly.

$$\begin{aligned} \text{Min } P_{CC}(k) \quad & \{ [-(1/n_{FC}(k)) * (P_{LOADS}(k) + P_{CC}(k) * n_{CC}(k))] + \\ & S * [C(k) - C_{NOM}]^2 \} \end{aligned} \quad (6)$$

A constant,  $S$ , is used to define the strength of the constraint and to indirectly set the boundaries of the

SOC window. The constraint encourages the choice of  $P_{CC}(k)$  to balance keeping the output of the fuel cell small as well as keeping the SOC close to the nominal SOC. From equation, it follows that:

$$5 \quad (C(k))^2 = (C(k-1))^2 - 2*C(k)*P_{CC}(k) + (P_{CC}(k))^2$$

and expanding equation (6) yields:

$$\begin{aligned} \text{Min } P_{CC}(k) \quad & \{[-(1/n_{FC}(k))*(P_{LOADS}(k) + P_{CC}(k)*n_{CC}(k))]\} \\ & + S*[(C(k-1))^2 - 2*C(k-1)*P_{CC}(k) + (P_{CC}(k))^2 \\ & - 2*(C(k-1) - P_{CC}(k))*C_{NOM} + C_{NOM}^2]\} \end{aligned} \quad (7)$$

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The gradient of equation (7) is taken with respect to  $P_{CC}(k)$  and is set to zero to yield the optimal  $P_{CC}(k)$ .

$$P_{CC}(k) = (n_{CC}(k)*V_{FC}^{MAX}) / (2*S*V_{FC}(k)) + C(k-1) - C_{NOM} \quad (8)$$

15 Now, given the system current loads and the equation for  $P_{CC}(k)$ , equation (5) can be rewritten as:

$$\begin{aligned} P_{FC}(k) = & -(V_{FC}^{MAX}/V_{FC}(k))*(P_{LOADS}(k) + \{(n_{CC}(k)*V_{FC}^{MAX}) / (2*S* \\ & V_{FC}(k)) + C(k-1) - C_{NOM}\}*n_{CC}(k)) \end{aligned} \quad (9)$$

Equation (9) can be rewritten as an equation for  $I_{FC}(k)$  by substituting in  $P_{FC}(k) = V_{FC}(k) * I_{FC}(k)$ ,  $P_{LOADS}(k) = V_{LOADS}(k) * I_{LOADS}(k)$  and by noting that  $V_{LOADS}(k) = V_{FC}(k)$ .

$$\begin{aligned} I_{FC}(k) = & -(V_{FC}^{MAX}/(V_{FC}(k))^2)*(V_{FC}(k)*I_{LOADS}(k) + \\ & \{(n_{CC}(k)*V_{FC}^{MAX}) / (2*S*V_{FC}(k)) + C(k-1) \\ & - C_{NOM}\}*n_{CC}(k)) \end{aligned} \quad (10)$$

Thus, two equations now exist for  $I_{FC}(k)$ , i.e. equation (1) and equation (10). Setting these equations equal to each other, various methods can be used to solve for  $V_{FC}(k)$ .

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For system loads 14 which supply power to the bus such as regenerative brakes, the fuel cell power is set to zero and the charge carrier 16 absorbs the power.

If  $P_{LOADS}(k) > 0$  then  $P_{FC}(k) = 0$ .

5 If the power system happens to be deigned such that it is possible for the system loads 14 to demand more power than can be supplied by the fuel cell 10, and the solved value for  $V_{FC}(k)$  is outside the limits, the fuel cell is commanded to the proper saturation point and the charge  
10 carrier 16 provides the additional power required.

If  $V_{FC}(k) > V_{FC}^{MAX}$  then  $V_{FC}(k) = V_{FC}^{MAX}$ .

If  $V_{FC}(k) < V_{FC}^{MIN}$  then  $V_{FC}(k) = V_{FC}^{MIN}$ .

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The inventive control method also simultaneously takes into account durability of the charge carrier 16. In the case of the use of a battery pack, the number of the charge/discharge cycles could be  
20 increased by maintaining the charge carrier SOC at a high level and reducing the SOC window. This can be done by adjusting the parameters  $C_{NOM}$  and  $S$ . The number of cycles available vs. the SOC window for a NiMH battery pack, for example, is an exponential  
25 relationship, but can be approximated by a quadratic over a section of the curve. Then, the quadratic cost function detailed above, which is a function of the SOC window, is similar to the exponential charge/discharge cycle "cost" function, which is also a function of the  
30 SOC window.

If the fuel cell is operated in its ohmic region only, then equation (1) can be re-written into a simplified linear equation in  $V_{FC}(k)$ .

$$I_{FC}(k) = (V_{FC}(k) - V_0) / S_0$$

5 Then, the following equation can be solved for  $V_{FC}(k)$  by using the above equation and equation (10).

$$\begin{aligned} (V_{FC}(k))^4 - V_0(V_{FC}(k))^3 + V_{FC}^{MAX} I_{LOADS}(k) S_0 (V_{FC}(k))^2 \\ + V_{FC}^{MAX} n_{CC}(k) (C(k-1) - C_{NOM}) S_0 V_{FC}(k) \\ + (V_{FC}^{MAX})^2 (n_{CC}(k))^2 S_0 / (2S) = 0 \end{aligned} \quad (11)$$

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If more than one solution is found to fall within the operating region of the fuel cell, then maximum real solution should be utilized.

The control method described above has been  
15 successfully verified in simulation tests performed using a hybrid fuel cell system operating in the ohmic region, and using a battery pack as the charge carrier. The initial conditions and constraints used in these tests were as follows:

$$\begin{aligned} 20 \quad P_{FC}^{MAX} &= 20,000 \text{ W} \\ V_{FC}^{MAX} &= 400 \text{ V} \\ V_{FC}^{MIN} &= 200 \text{ V} \\ V_{FC}^{MAX \text{ POWER}} &= 400 \text{ V} \\ C_{NOM} &= 1,000 \\ 25 \quad C(0) &= 1,000 \\ S &= 1 \\ n_{PC} &= 0.9 \\ e_{CC} &= 0.9 \\ V_0 &= 400 \text{ V} \\ 30 \quad S_0 &= -2 \end{aligned}$$

Figs. 2-6 are waveform plots showing electrical operating parameters for the fuel cell system used in the simulation tests. Fig. 2 is a plot of the  
35 total commanded system load current as a function of

time. The negative value of the current shown in Fig. 2 indicates that the loads were acting a current sink.

Figs. 3a and 3b respectively show the computed  
5 values of the voltage and current output by the fuel  
cell, based on the calculated battery pack power. The  
current originates from the ohmic region of the  
polarization curve. Fig. 4 is a plot of the fuel cell  
output power, and Fig. 5 is a plot of the battery pack  
10 output power. Fig. 5 shows that the battery pack is  
cyclically sourcing and sinking power. Fig. 6 is a plot  
showing the battery pack SOC, and demonstrates that the  
SOC stayed within a desired band of charge, but changes  
over time due to changing power demands on the battery  
15 pack.

Fig. 7 is a simplified flowchart showing each  
of the basic steps of the inventive method. The method  
starts at step 20 with the determination of the current  
20 state of charge of the charge carrier 16. A  
determination is also made at step 22 of the maximum  
amount of power that can be output by the fuel cell 10.  
At step 24, a determination is made of the amount of  
power currently being output by the fuel cell 10. Steps  
25 20-24 may be performed by direct measurement, or by  
inference based on other available data and information.  
Then at step 26, a determination is made of whether the  
power being currently demanded by the load 14 is less  
than the maximum power output of the fuel cell 10. If  
30 the answer is yes, the charge carrier output is set to a  
first value determined by equations previously  
described. But if the answer is no, then the charge  
carrier output is set to a second value which is also  
determined by the previously explained equations. As

shown at 32, the method steps are then repeated, based on the using the previous SOC.

5       It is to be understood that the specific method and techniques which have been described are merely illustrative of one application of the principle of the invention. Numerous modifications may be made to the method as described without departing from the true spirit and scope of the invention.

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